Janta model for the ferroelectric hysteresis loop

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Jiri Janta (1971) The influence of the shape of domains on the ferroelectric hysteresis loop, Ferroelectrics, 2:1, 299-302,

Polarization reversal



Fig. 1

(a) Domain switching behavior for (upper) metal-ferroelectric-metal and (lower) AFM tip-ferroelectric-metal structures. (b) PFM phase image of dot-patterned domains formed by negative voltage pulses to the bottom electrode in 90-nm-thick P(VDF-TrFE) thin films.

Strongly simplifying models based on the sideways expansion of 180" domains

Assumptions:



Strip domains: Surface density of nuclei N₂ Initial domain half-width d₀



FIG. 2. Scheme demonstrating the variants of domain growth dimensionality: (a) the growth of the lamella domains in finite media, (b) the growth of cylinder domains in finite media

The velocity of the sideways motion of the domain walls is $v = v_{\infty} \exp(-\alpha/E)$

Eq. 1

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- α The activation field
- v_{∞} The extrapolated wall velocity for $E = \infty$



FIG. 2. Logarithm of the sidewise 180° domain-wall velocity vs the reciprocal of the applied electric field for a sample 4.0×10^{-3} cm thick. The dotted line is an extrapolation of the straight line drawn through the data for $v > 10^{-4}$ cm sec⁻¹.

Journal of Applied Physics 31, 662 (1960); https://doi.org/10.1063/1.1735663

Cylindrical domains: Surface density of nuclei N₁ Initial radius of domains r₀

Strip domains: Surface density of nuclei N₂ Initial domain half-width d₀

 $v = v_{\infty} \exp(-\alpha/E)$

Applied field: $E = E_0 \sin(wt)$ Increased domain area:

Cylindrical domain: $\pi (r_0 + \int v dt)^2 = \pi (r_0 + v_\infty \int \exp(-\frac{\alpha}{E_0 \sin(wt)}) dt)^2 = \pi (r_0 + \frac{v_\infty}{w} I(wt, \frac{E_0}{\alpha}))^2$ Strip domain: $2 \left[d_0 + \frac{v_\infty}{w} I(wt, \frac{E_0}{\alpha}) \right]$

$$I(\omega t, E_0/\alpha) = \int_0^{\omega_l} \exp\left(-\frac{\alpha}{E_0 \sin x}\right) dx,$$

The areas of reversed polarization per unit area:

$$a_{1\text{ex}}(\omega t) = \pi N_1 \left[r_0 + \frac{v_\infty}{\omega} I(\omega t, E_0/\alpha) \right]^2, \quad (2')$$

$$a_{2\text{ex}}(\omega t) = 2N_2 \left[d_0 + \frac{v_\infty}{\omega} I(\omega t, E_0/\alpha) \right], \quad (2'')$$

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The mutual overlap of growing domains is described by the equation⁷:

$$a(\omega t) = 1 - \exp\left(-a_{ex}(\omega t)\right), \qquad (3)$$

(assumption of random distribution of grain centers throughout the volume)

$$a_{1}(\omega t) = 1 - \exp\left(-\pi N_{1}\left[r_{0} + \frac{\nu_{\infty}}{\omega}I\left(\omega t, \frac{E_{0}}{\alpha}\right)\right]^{2}\right)$$





Cylindrical domains:

$$a_{1}(\omega t) = 1 - \exp\left(-\pi N_{1}\left[r_{0} + \frac{v_{\infty}}{\omega}I\left(\omega t, \frac{E_{0}}{\alpha}\right)\right]^{2}\right)$$
$$\frac{P(\omega t)}{P_{s}} = 2a(\omega t) - 1.$$
$$\frac{P_{1}(\omega t)}{P_{s}} = 1 - 2\exp\left\{-\pi N_{1}[r_{0} + \frac{v_{\infty}}{\omega}I(\omega t, E_{0}/\alpha)]\right\}^{2}\right\}$$



where r_0 is given by the symmetry condition $P(\pi) = -P(0)$

$$\exp\{-\pi N_1 \left[r_0 + \frac{v_{\infty}}{\omega} I(\pi, E_0/\alpha)\right]^2\} + \exp(-\pi N_1 r_0^2) = 1 \qquad \delta = \sqrt{N_1} * v_{\infty}/w$$

(5')

7. M. Avrami, J. Chem. Phys. 8, 212 (1940).

Strip domains:

$$\frac{P_2(\omega t)}{P_s} = 1 + \left\{ 1 + \tanh\left[N_2 \frac{v_\infty}{\omega} I(\pi, E_0/\alpha)\right] \right\} \\ \times \exp\left[-2N_2 \frac{v_\infty}{\omega} I(\omega t, E_0/\alpha)\right].$$

$$\delta = \sqrt{N_1} * v_{\infty} / w$$



FIGURE 1. Halves of hysteresis loops computed using the models of cylindrical domains (full line, $\delta = (v_{\infty}/\omega)\sqrt{N_1}$) and strip domains (dashed line, $\delta = v_{\infty}N_2/\omega$): (a) for various amplitudes of the electric field, (b) for various values of the parameter δ inversely proportional to the frequency.

Application of Janta model



Figure 4. Dielectric hysteresis loops in an MBI single crystal for f = 50 Hz and different values of the amplitude Emax of the applied field for T = 350 K (a) and T = 381 K (b). The lines show the simulations. Dependence of the maximum polarization Pmax and remnant polarization Prem on the amplitude of the applied field for f = 50Hz, T = 334 K (c). Temperature dependence of coercive field Ec for f = 30 Hz and 200 Hz, Emax = $2.4 V/\mu$ (d).

Т, К

In summary

Janta model is just a particular case of Kolmogorov-Avrami-Ishibashi (KAI) model. The KAI model assumes either a constant nucleation rate during switching (category I) or only latent nuclei and no new nucleation during switching (category II), leading to different effective dimensionalities (n).

KAI model:

$$P(t) = 2P_{S}\{1 - \exp[-(t/t_{0})^{n}]\},\$$

Janta model:

$$\frac{P_1(\omega t)}{P_s} = 1 - 2 \exp\left\{-\pi N_1 \left[r_0 + \frac{v_\infty}{\omega} I(\omega t, E_0/\alpha)\right]\right\}^2\right\}$$

THANK YOU!